

PSBB Learning Leadership Academy
Bangalore
Mathematics

Class 8

Cubes & cube roots

1 a) $\left(\frac{1}{2}\right)^3 = \frac{1}{8}$

b) $\left(2\frac{7}{9}\right)^3 = \left(\frac{25}{9}\right)^3$
 $= \frac{15625}{729}$

c) $(54)^3 = 157464$

d) $(-1)^3 = -1$

e) $(4.3)^3 = 79.507$

2) a) $\sqrt[3]{6859} = 19$

b) $\sqrt[3]{24 \times 36 \times 80 \times 25} = \sqrt[3]{\underline{8} \times 3 \times 9 \times \underline{4} \times \underline{8} \times 5 \times \underline{5}^2 \times \underline{2}}$
 $= \sqrt[3]{8^3 \times 3^3 \times 5^3}$
 $= 8 \times 3 \times 5$
 $= 120$

c) $\sqrt[3]{\frac{3375}{125}} = \sqrt[3]{\frac{25 \times 27 \times 5}{25 \times 5}} = 3$

d) $\sqrt[3]{1.331} = 1.1$

$$\begin{array}{r}
 2 \overline{) 1944} \\
 2 \overline{) 972} \\
 2 \overline{) 486} \\
 3 \overline{) 243} \\
 3 \overline{) 81} \\
 3 \overline{) 27} \\
 3 \overline{) 9} \\
 3 \overline{) 3} \\
 1
 \end{array}$$

$1944 = 2^3 \times 3^3 \times 3^2$
 It's not a perfect square

$$\begin{array}{r}
 5 \overline{) 10985} \\
 13 \overline{) 2197} \\
 13 \overline{) 169} \\
 13 \overline{) 13}
 \end{array}$$

$$10985 = 5 \times 13^3$$

$$\frac{10985}{5} = \frac{5 \times 13^3}{5}$$

$\therefore 10985$ should be divided by 5

$$\boxed{2197 = 13^3}$$

$$5) \quad 200 = 2 \times 10 \times 10$$

$$200 \times 2^2 \times 10 = 2 \times 2^2 \times 10$$

40 should be multiplied to make it a perfect cube

$$\begin{aligned}
 6) \quad a) \quad \sqrt[3]{4^3} \times \sqrt[3]{6^3} &= 4 \times 6 \\
 &= 24
 \end{aligned}$$

$$\begin{aligned}
 b) \quad \sqrt[3]{1000} + \sqrt[3]{0.008} - \sqrt[3]{0.125} &= 10 + 0.2 - 0.5 \\
 &= 10.2 - 0.5 \\
 &= 9.7
 \end{aligned}$$

$$c) \quad \sqrt[3]{0.1 \times 0.1 \times 0.1} = 0.1$$

(8) Area of one face = 64 cm^2
 $s^2 = 64 \text{ cm}^2$
 $s = 8 \text{ cm}$
 Volume = s^3
 $= 512 \text{ cm}^3$

(9) Example
 $18^3 = 18 \times 18 \times 18$
 $= 18 \times 3 \times 6 \times 18$
 $= 54 \times 3 \times 18 \times 2$
 $= 54 \times 54 \times 2$
 multiples of 27

10 $(x^2)^3 = 729$
 $(x^2)^3 = (9)^3$
 $= (3^2)^3$

$\boxed{\sqrt{9} = 3}$

11 Let the nos be $2x, 3x, 4x$

$$(2x)^3 + (3x)^3 + (4x)^3 = 33957$$

$$8x^3 + 27x^3 + 64x^3 = 33957$$

$$99x^3 = 33957$$

$$x^3 = \frac{33957}{99}$$

$$x^3 = 343$$

$$\therefore x = 7$$

$\therefore$ nos are $14, 21, 28$

12) (a) $\overbrace{389}^{G_2} \overbrace{017}^{G_1}$

$\therefore G_1$ has 7 in unit place then unit digit should be 3

G_2 389 lies between 7^3 & 8^3

$$\therefore \sqrt[3]{389017} = 73$$

$$\textcircled{b} \sqrt[3]{226981} = 61$$

13

$$\begin{aligned} \text{Volume of Big cube} &= 20^3 \text{ cm}^3 \\ \text{Volume of 1 small cube} &= 5^3 \end{aligned}$$

$$\begin{aligned} \text{No. of cubes} &= \frac{\text{V. of Big cube}}{\text{V. of small cube}} \\ &= \frac{20 \times 20 \times 20}{5 \times 5 \times 5} \\ &= 64 \end{aligned}$$

14

$$\text{Dimensions of matbox} = 4 \text{ cm} \times 2.5 \times 1.5 \text{ cm}$$

$$\begin{aligned} \text{Volume of big cube} &= 2^2 \times 2.5 \times 1.5 \times 2 \times (2.5)^2 \times (1.5)^2 \\ &= 2^3 \times (2.5)^3 \times (1.5)^3 \end{aligned}$$

$$\text{Dimensions of new cube} = 8 \times 15.625 \times 3.375$$

15) 20 cubes required to make a cube of edge 3 units